

Compression of Measured 2D UWB Antenna Transfer Functions

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Abstract

We derive rules of thumb for compressing transfer functions of UWB antennas using a phase-mode/Slepian-mode based model. The are applied to measured 2D UWB radiation patterns of bowtie, log-periodic and Vivaldi antennas. A compression ratio of 5.8 with a maximal error of 10% is achieved.

Introduction Stemming from military radar applications, Ultra Wideband (UWB) communications (systems with a relative bandwidth in excess of 0.2 times the center frequency f_c or with absolute bandwidth larger than 500 MHz) are being researched intensively in both academic and industrial environments. In 2002 the FCC licensed UWB communication between 3.1 GHz and 10.6 GHz, with a spectral mask of -41 dB/MHz, [1], while in 2007 the European Commission allowed UWB communication between 6.0 GHz and 8.5 GHz. Because of the large bandwidths, antenna parameters can no longer be considered constant over frequency. Hence, in a UWB system, the frequency dependency of all parameters should be carefully taken into account, resulting in a large increase of data to be manipulated. [2] proposed an efficient model to compress the 3D transfer function of an antenna without loss of accuracy. The main advantage of this model over more traditional rational modeling methods, is that it allows to reduce the noise contribution in the data, provided truncation boundaries are chosen correctly. In this letter, we define rules of thumb for these truncation

boundaries and apply them to measured 2D UWB radiation patterns of bowtie, log-periodic and Vivaldi antennas.

Compression Ratio We consider the measured vector transfer function of an antenna, which relates the input pulse to the radiated field, as defined in [3]. In this letter elevation angle is held constant at θ_0 . Since both polarisations can be treated independently we focus on a scalar transfer function $H(\theta_0, \phi, f)$. The model [2] expands the azimuthal dependency into phase modes and the frequency dependency into Slepian modes:

$$H(\theta_0, \phi, f) = \sum_{m=-M}^M \sum_{k=0}^K H_{m,k}^{\phi,f}(\theta_0) \psi_{k,c}(f) \exp(jm\phi) \quad (1)$$

where $\psi_{k,c}(f)$ is the k -th order DPSS with bandwidth parameter c .

As for the compression ratio of the *phase modes*, first note that the transfer function is closely related to the radiation pattern:

$$\frac{\mathbf{F}(\theta, \phi, f)}{\sqrt{Z_0}} = \frac{\mathbf{H}(\theta, \phi, f)}{2\pi c_0} \cdot j\omega \frac{U(f)}{\sqrt{Z_c}} \quad (2)$$

The radiation pattern in the frequency domain is identical to the transfer function, up to a constant factor. From [4], we know that the energy contained in the m -th phase mode decreases rapidly when $m > k_0 r$, with $k_0 = 2\pi/\lambda$ and λ the wavelength. As a rule of thumb we now choose the truncation boundary at $m = \lceil k_0 d \rceil + 4$, with d the largest dimension of the antenna and k_0 the wavenumber of the largest frequency under consideration.

To deduct a rule of thumb for the amount of *Slepian Modes* needed to represent an antenna transfer function we apply some properties of the DPSS derived by Slepian, [5]. Given that the DPSSs are the eigenvectors of the sinc-matrix

$$B(N, c)_{k,l} = \frac{\sin(2\pi c (k-l))}{\pi (k-l)}, \quad (3)$$

where $0 < c < 0.5$ is the bandwidth parameter and N the total number of frequency samples, for the corresponding eigenvalues, we find that $1 > \lambda_0 > \lambda_1 > \lambda_2 > \lambda_3 > \dots \lambda_n > 0$. These λ_i are almost 1 for $i \leq 2cN$ and almost 0 for $i > 2cN$. As these λ_i also represent the fraction of the spectral energy of the i -th order DPSS in $|f| < BW$, with BW the bandwidth on which the DPSS are defined, Parseval's theorem dictates that all BW -bandlimited functions are described accurately using only the first $2cN$ DPSSs. Since there is a small transitional area where the λ_i cannot be considered close to 1 or 0, it is advisable to use $K > 2cN$. When $K = \lceil 2cN \rceil + 14$, accuracies over 90% can be achieved. For large N the influence of this transitional region in the eigenvalues is negligible, but for smaller N it is important to add the extra 14 modes.

Validation To validate these results three different UWB antenna transfer functions, measured at the Universität Karlsruhe [3], were compressed: a bowtie antenna, a log-periodic antenna and a vivaldi antenna. All antennas were measured from 0.4 GHz to 20 GHz at 801 frequency points, using 91 samples in the azimuthal plane. Given that all antennas were measured in the same frequency range, they are expanded into an equal amount of Slepian modes: $801 \times 0.1254 \times 2 + 14 = 214$, using $c = 0.1254$ as in [2]. The bowtie antenna has dimensions $36 \times 31 \text{ mm}^2$, requiring $0.036 \times 20e9/3e8 \times 2\pi + 4 = 20$ phase modes. In Figure 1 the phase- and Slepian mode coefficients are shown. It is easily verified that the energy at the truncation boundaries is close to zero. For the Vivaldi antenna, measuring $75 \times 78 \text{ mm}^2$, we need 37 phase modes. The logperiodic antenna with dimensions $60 \times 50 \text{ mm}^2$ is modelled by 30 phase modes. The total number of coefficients needed to describe the frequency response reduces from 72891 to 12626 on average: a reduction by a factor of about 5.8.

The relative errors, between the original transfer function $H(\theta_0, \phi, f)$ and the reconstructed $\hat{H}(\theta_0, \phi, f)$ is defined as $\sum_{\phi} \left| H(\theta_0, \phi, f) - \hat{H}(\theta_0, \phi, f) \right| / \sum_{\phi} |H(\theta_0, \phi, f)|$ and are shown in Figure 2. We see that all the error curves are very close to

each other and below 10% error for almost all frequencies. This can also be verified on Figure 3, where both the original and reconstructed transfer function, for $\phi = 0$, is plotted for all three antennas.

Conclusion Strategies for the accurate prediction of the truncation boundaries of a model for the antenna frequency response using phase and Slepian modes were derived. These rules of thumb were then verified on three measured UWB antennas with a different radiation mechanisms. Using this model the size of the frequency response was compressed by factor of about 5.8 with a relative error below 10%.

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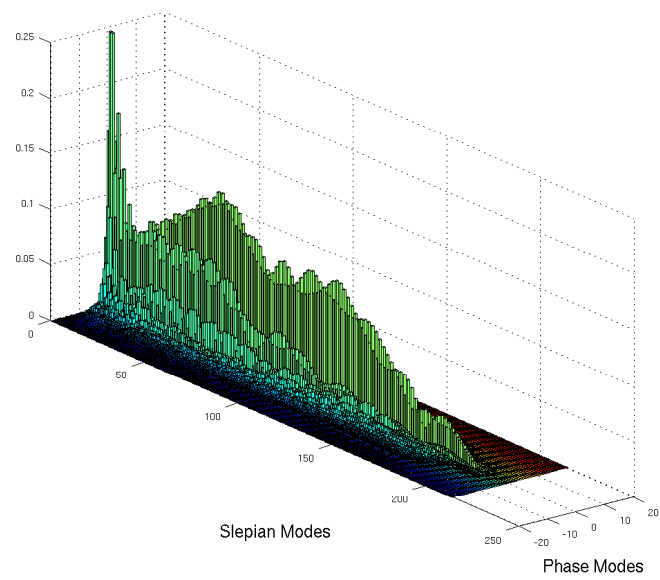


Figure 1: Model coefficients of the bowtie antenna

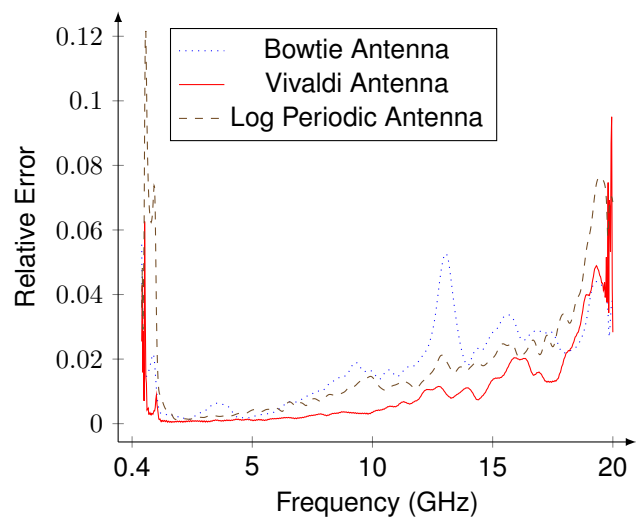


Figure 2: Relative error

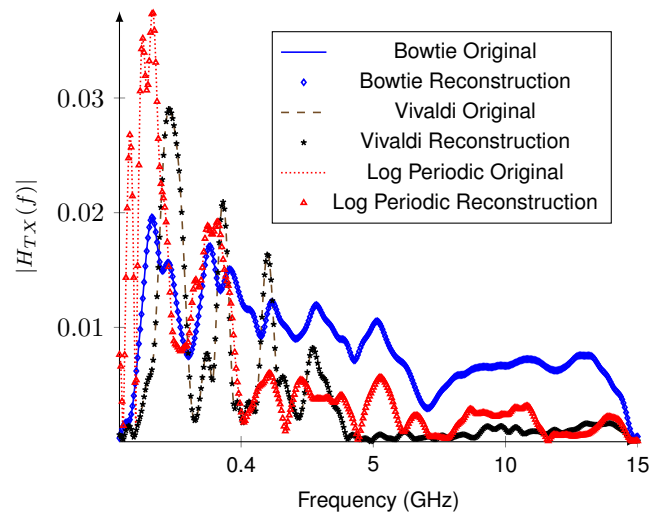


Figure 3: Antenna transfer function for $\phi = 0$